



# A Logical Pattern Memory Pre-trained Model for Entailment Tree Generation

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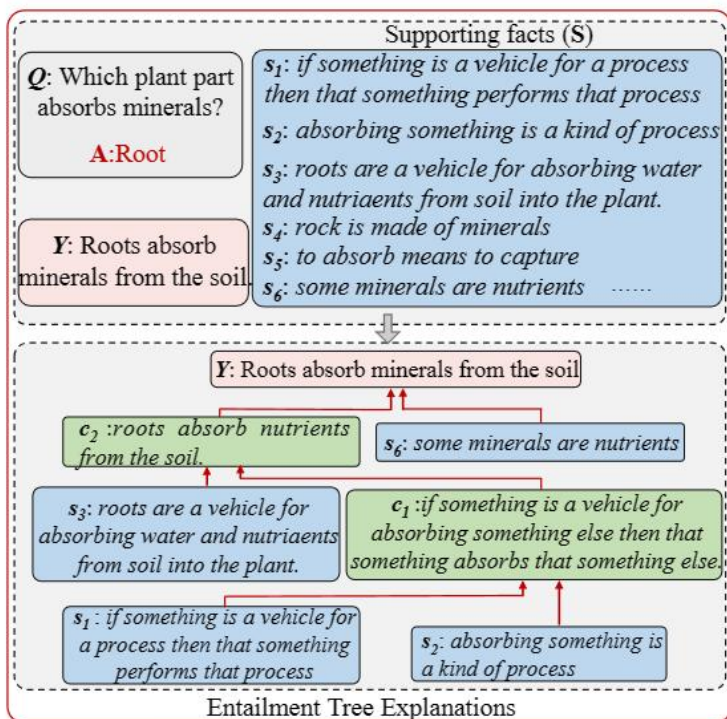


Figure 1: Illustration of Entailment Tree Generation. The top half presents the inputs, while the generated entailment tree is depicted in the bottom half. The tree consists of a hypothesis (pink), premises (blue), and generated intermediate conclusions (green).

Generating coherent and credible explanations poses a significant challenge in AI, and addressing it represents a giant leap towards the goal of **building reliable reasoning systems**.

In recent years, researchers have explored the utilization of **entailment trees for explanation generation**.

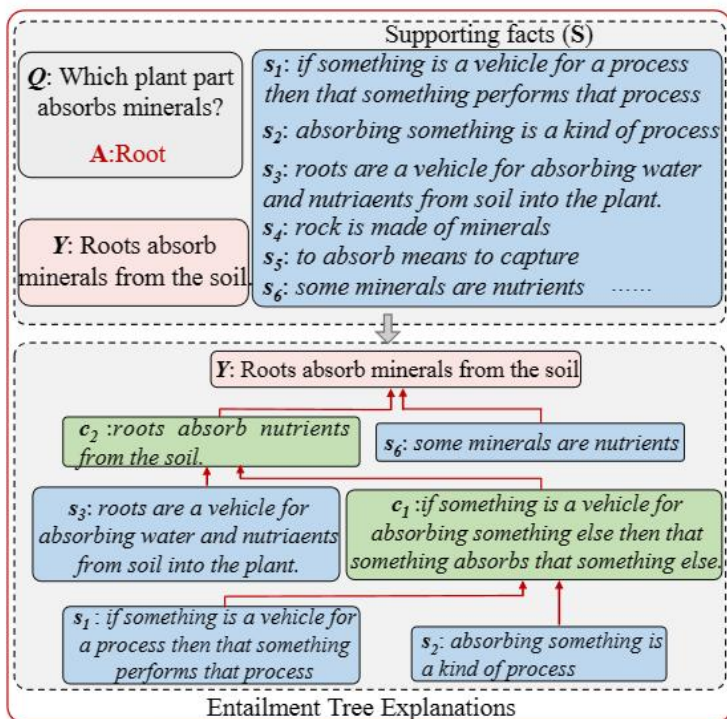


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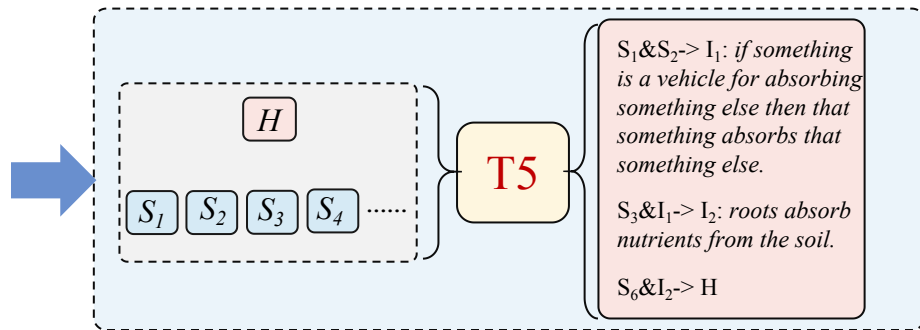
In recent years, researchers have explored the utilization of **entailment trees for explanation generation**.

The task of entailment tree generation **can be defined as follows**: given a hypothesis (summarizing from a question+answer pair) and a set of supporting facts, the goal is to derive an entailment tree where each non-leaf node is an intermediate conclusion generated from its children



### Previous works

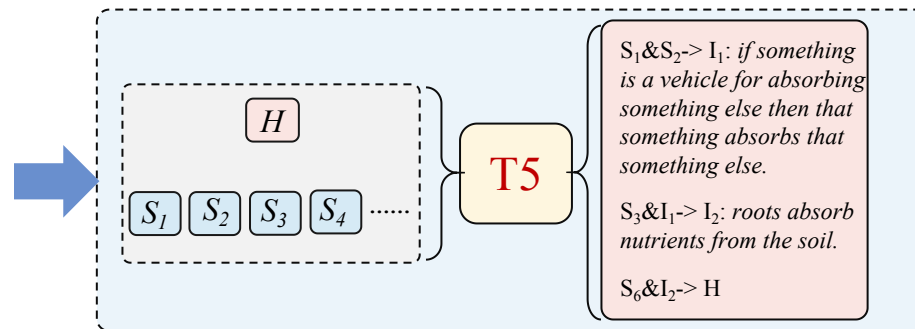
#### 1. Single-step method[1]



**Drawback:** Unreliable explanations for the hypothesis[2]

### Previous works

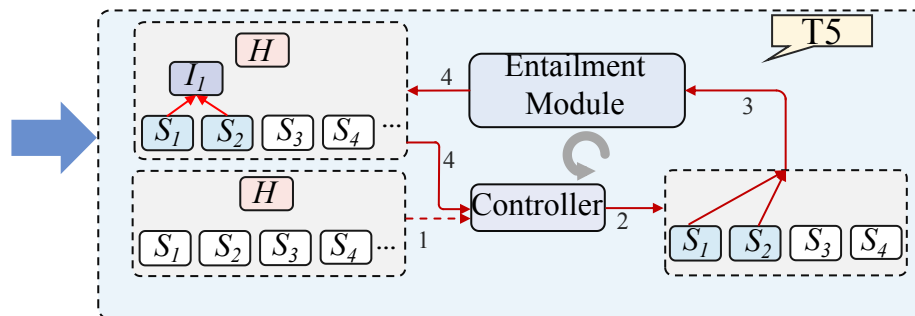
#### 1. Single-step method[1]



#### Drawback:

Unreliable explanations for the hypothesis[2]

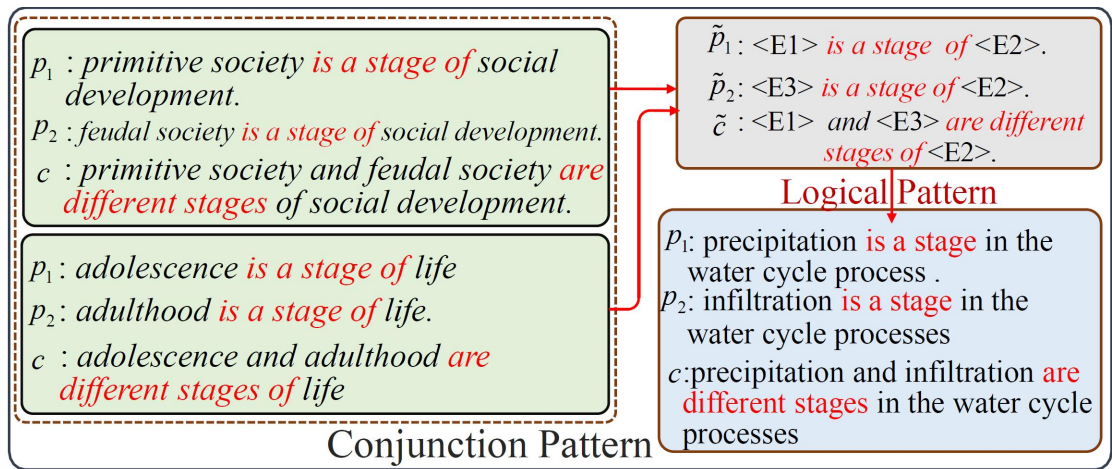
#### 2. multi-step generation method [3-6]



#### Drawback:

Iterative methods lies in their limited attention to the logical patterns between premises and conclusions

## METGEN



### Drawbacks:

1. During training, the **language model** is forced to learn **both logical patterns and textual features**, which dilutes its focus on capturing logical patterns.
2. Using Wikipedia data as a training resource introduces a considerable amount of **domain-specific information that isn't logically relevant**.

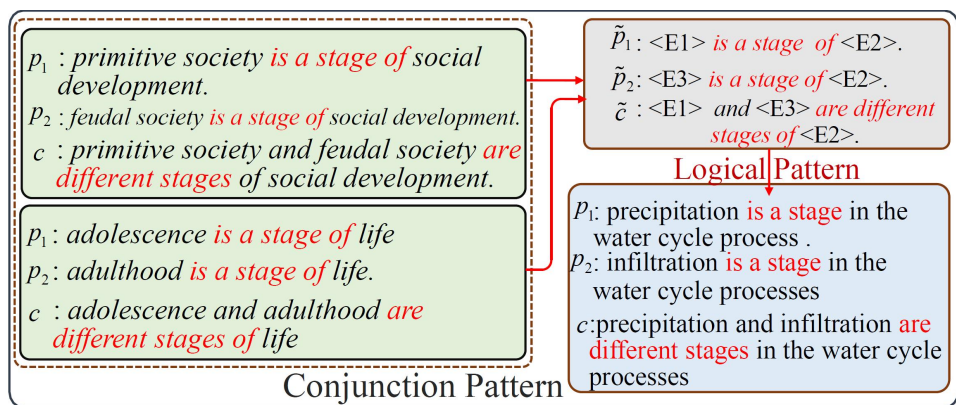
Although, METGEN [3] stands out for its attempt to integrate **logical patterns** into the tree generation process.

METGEN's strategy for integrating logical patterns involves training the language model on a synthetic dataset constructed from Wikipedia (**Green boxes**).

## Our Method

**Key:** Map the implicit **logical patterns onto the embedding space.**

## 1. Entity abstraction techniques



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**1. Entity abstraction techniques**

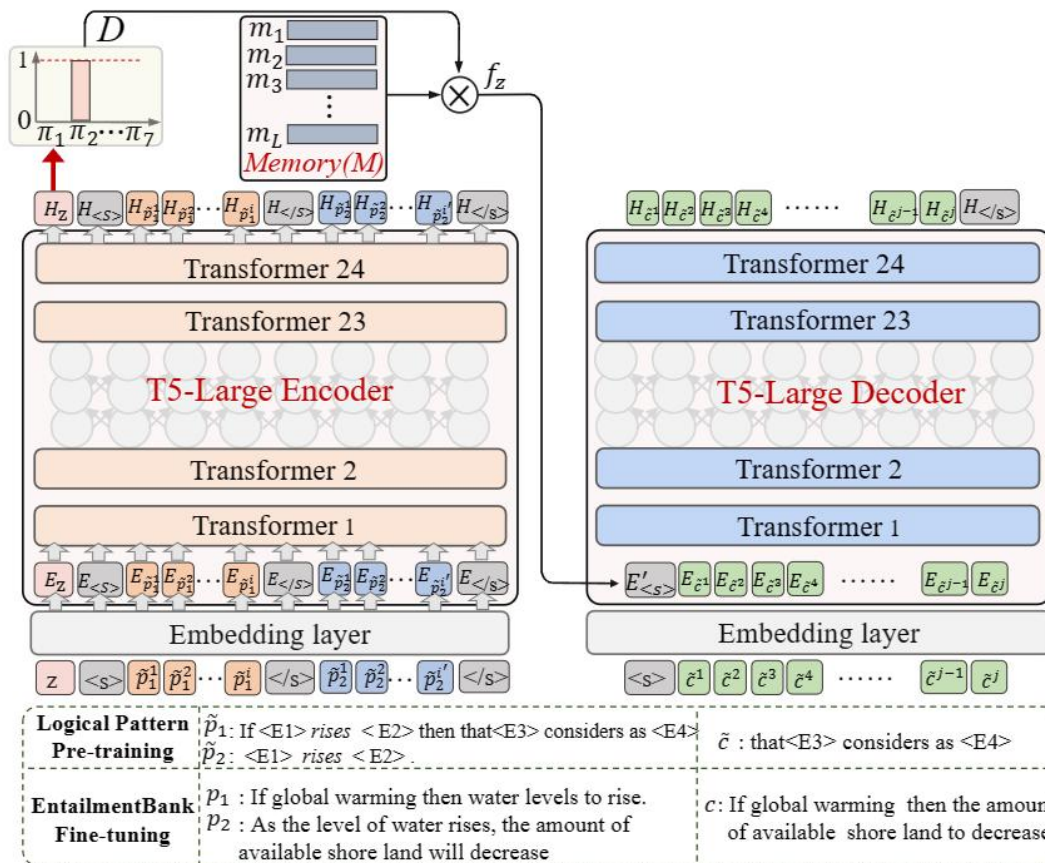
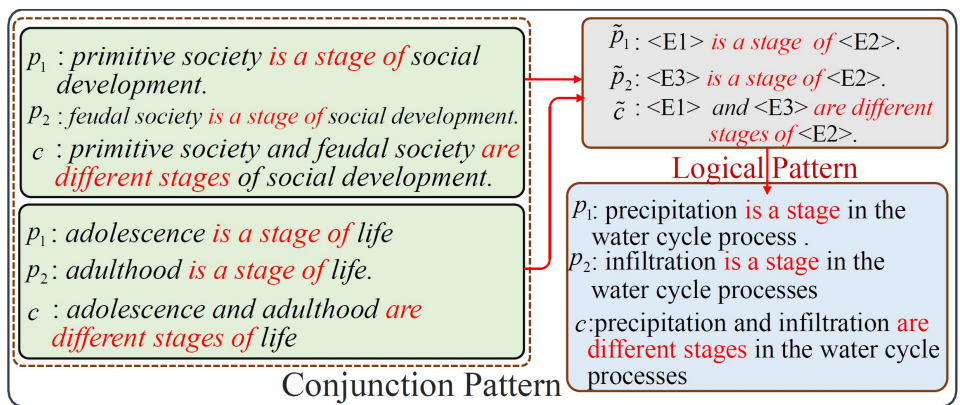


Figure 3: The overall architecture of LMPM

**A Logical Pattern Memory Pre-trained Model**



## Step 1: Logical Pattern Pre-training

Enhance its ability to capture and learn latent logical pattern

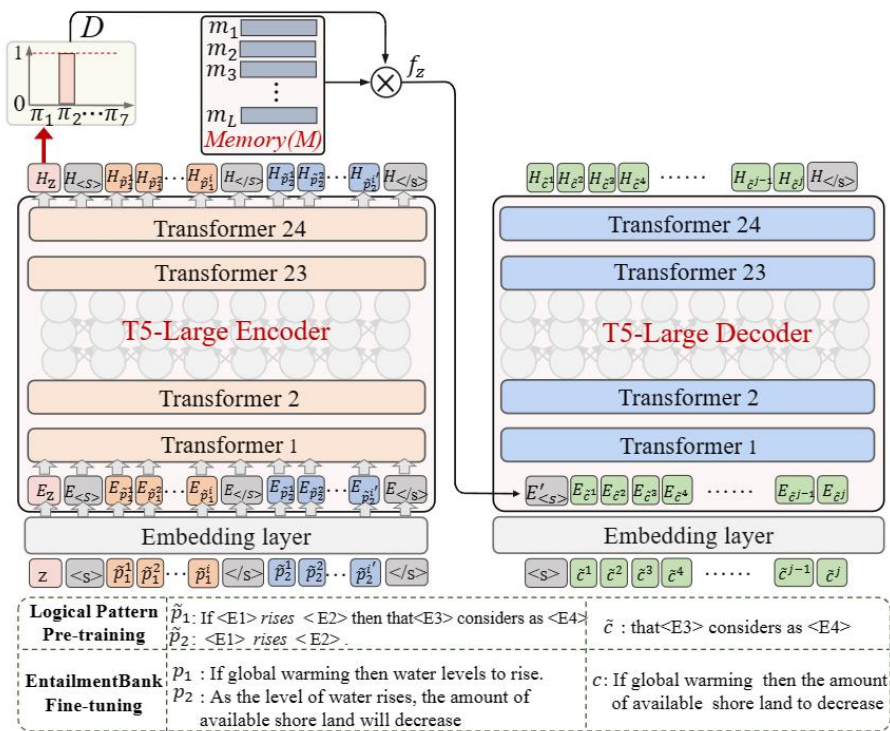


Figure 3: The overall architecture of LMPM

$$I_{\text{logical}} = [\langle z \rangle, \langle s \rangle, \tilde{p}_1^1, \dots, \tilde{p}_1^L, \langle /s \rangle, \tilde{p}_2^1, \dots, \tilde{p}_2^L, \langle /s \rangle]$$

$$M = [m_1, \dots, m_L] \in \mathbb{R}^{L \times d_m}$$

where, each element  $m_i$  in  $M$  indicates a specific logical pattern

Then, we introduce an address structure  $D$ , which employs a multi-layer perceptron architecture.

$$\gamma_i = w_z H_z + b_z$$

**Gumbel-softmax**

$$\alpha_i = \frac{\exp(\gamma_i + g_i) / \mathcal{T}}{\sum_{i=1}^L \exp(\gamma_i + g_i) / \mathcal{T}}$$

This structure takes  $H_z$  as input and produces a one-hot vector to help locate the potential logical pattern representation in  $M$ .

$$f_z = \sum_{i=1}^L \alpha_i M_i$$



## Step 1: Logical Pattern Pre-training

we integrate the selected logical pattern representation into the T5-decoder by adding it to the representation of the start special token <s>.

$$E'_{\langle s \rangle} = f_z + E_{\langle s \rangle}$$

### Loss Function:

1. language modeling loss (LM)

$$\mathcal{L}_{LM} = - \sum_{t=1}^{|\tilde{c}|} \log p(\tilde{c}^t | f_z, \tilde{p}_1, \tilde{p}_2, \tilde{c}^{0:t-1})$$

2. To tackle the issue of vanishing latent variables a bag-of-words loss (BOW)

$$\mathcal{L}_{BOW} = \sum_{t=1}^{|\tilde{c}|} \log p(\tilde{c}^t | f_z, \tilde{p}_1, \tilde{p}_2) = \sum_{t=1}^{|\tilde{c}|} \log \frac{e^{f(\tilde{c}^t)}}{\sum_{v \in V} e^{f(v)}}$$

$$\mathcal{L} = \mathcal{L}_{LM} + \mathcal{L}_{BOW}$$

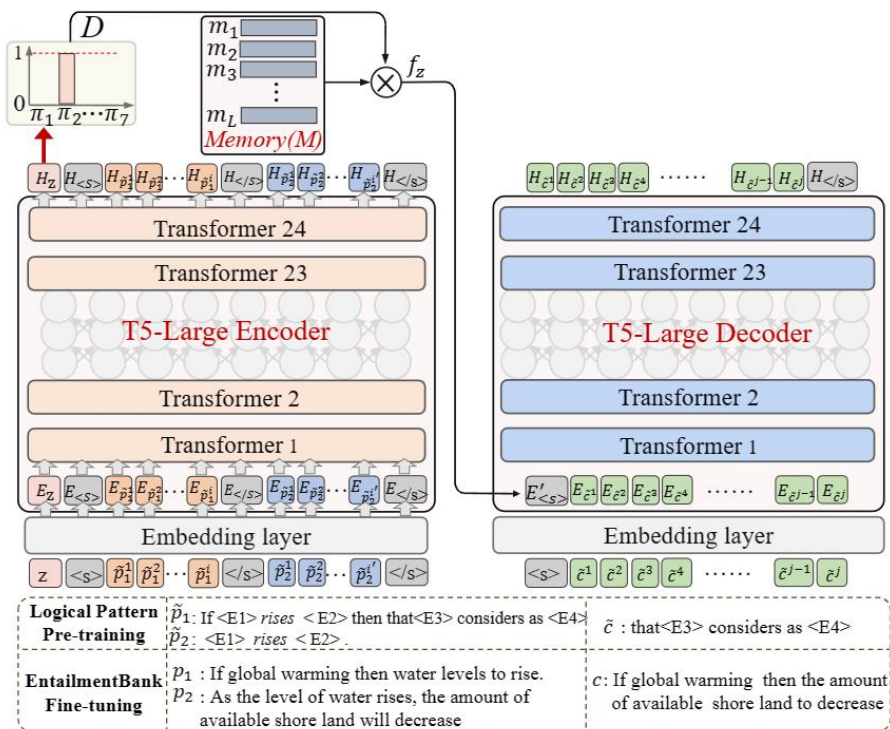


Figure 3: The overall architecture of LMPM



## Results

Method	Additional Data	Leaves		Steps		Intermediates		Overall AllCorrect
		$F_1$	AllCorrect	$F_1$	AllCorrect	$F_1$	AllCorrect	
Task1								
EntailmentWriter(T5-large)	No	98.4	84.1	50.0	38.5	67.0	35.9	34.4
IRGR	No	97.6	89.4	50.2	36.8	62.1	31.8	32.4
RLET	No	<b>100.0</b>	<b>100.0</b>	55.0	41.2	67.2	36.7	35.1
METGEN+T5	564K	<b>100.0</b>	<b>100.0</b>	<u>57.7</u>	<u>41.9</u>	<u>70.8</u>	<u>39.2</u>	36.5
<b>METGEN+LMPM(ours)</b>	564K	<u>99.76</u>	<u>99.41</u>	<b>57.78</b>	<b>43.82</b> †	<b>72.78</b> †	<b>42.78</b> †	<b>38.54</b> †
Task2								
EntailmentWriter(T5-large)	No	<b>83.2</b>	35.0	39.5	24.7	<b>62.2</b>	28.2	23.2
IRGR	No	69.9	23.8	30.5	22.40	47.70	26.5	21.8
RLET	No	81.9	40.4	38.8	28.7	57.4	29.1	26.0
METGEN+T5	564K	<u>82.7</u>	<u>46.1</u>	<u>41.3</u>	<u>29.6</u>	61.4	<u>32.4</u>	<u>27.7</u>
<b>METGEN+LMPM(ours)</b>	564K	81.09	<b>47.06</b>	<b>42.56</b>	<b>31.38</b> †	<u>61.68</u>	<b>34.32</b> †	<b>29.41</b> †
Task3								
EntailmentWriter(T5-large)	No	30.9	1.2	4.4	1.2	28.8	5.6	1.2
IRGR	No	<b>46.6</b>	<u>10.0</u>	<u>11.3</u>	8.2	<u>38.7</u>	<b>20.9</b>	8.2
RLET	No	<u>46.20</u>	<b>11.41</b>	<b>15.2</b>	<b>9.6</b>	<b>41.4</b>	17.6	<u>9.4</u>
METGEN+T5	564K	34.8	8.7	9.8	8.6	36.6	<u>20.4</u>	8.6
<b>METGEN+LMPM(ours)</b>	564K	35.3	9.23	10.28	<u>9.23</u>	37.8	20.33	<b>9.41</b>

Table 2: Automatic evaluation results on the EntailmentBank dataset (%). The best and second-best results are highlighted in bold and underlined, respectively. † refers to significance test  $p - value < 0.05$ . The “Additional Data” column denotes the size of the supplementary Wikipedia training data.

Mtrics	METGEN+T5	METGEN+LMPM
Validity	46	52
Logical	3.02	3.37
Readability	4.11	4.43
Reasonability	3.37	3.64

Table 3: Human evaluation results on 100 uniformly sampled questions from the test split.



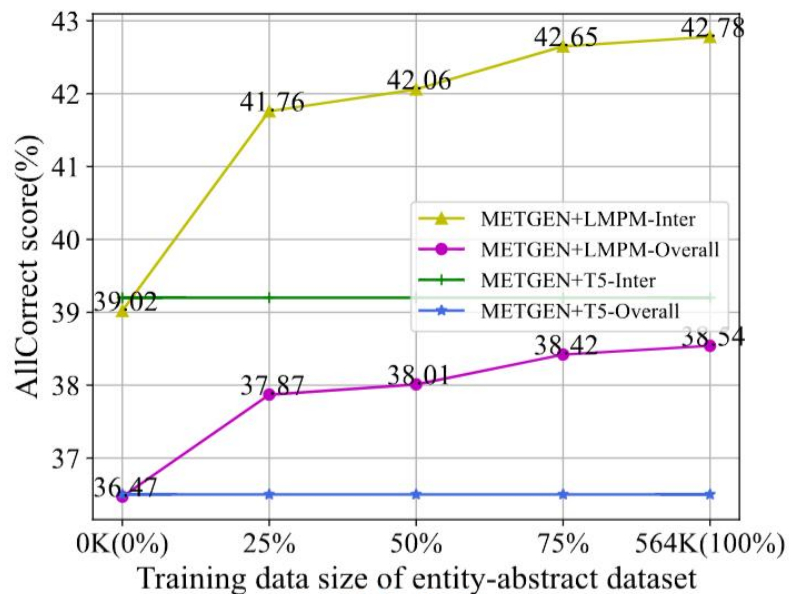
## Ablation Study

Method	Task 1		Task 2	
	Inter	Overall	Inter	Overall
METGEN+T5	39.2	36.5	32.4	27.7
METGEN+LMPM	42.78	38.54	34.32	29.41
<i>w/o LPP</i>	39.02	36.47	32.24	27.56
<i>w/o memory</i>	40.59	37.39	33.06	28.54
<i>w/o abstraction</i>	41.27	37.45	33.78	28.48

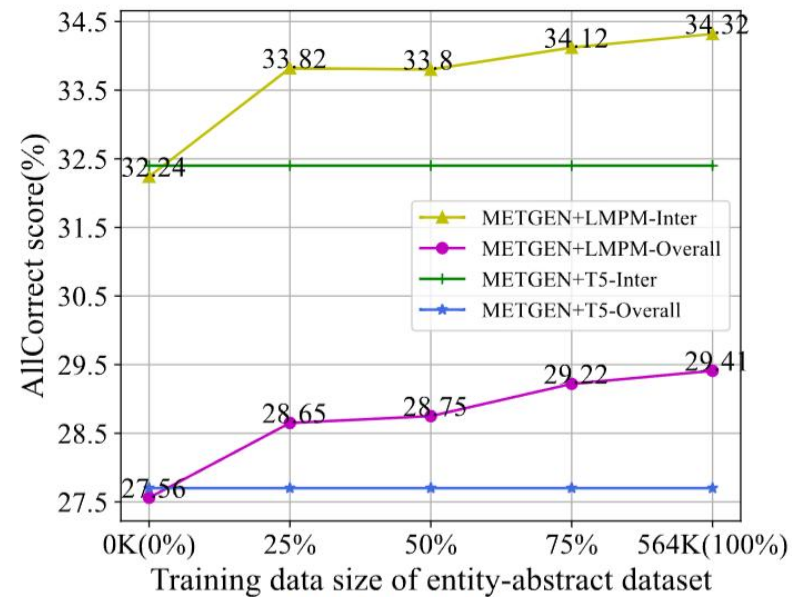
Table 4: Ablation study results. “Inter” and “Overall” denote Intermediates AllCorrect and Overall AllCorrect, respectively.

Three parts: logical pattern pre training (LPP), memory structure (memory), and dataset abstraction (abstraction)

## Logical Pattern Data Size



(a) Task 1.



(b) Task 2.

Figure 5: The impact of logical pattern pre-training data size on performance. The AllCorrect scores for Overall and Inter (Intermediates) are provided.

## Additional Analysis

Substitution	0.0714	0.0549	0.4475	0.0989	0.0439	0.0549	0.2282
Conjunction	0.0458	0.0917	0.1802	0.0825	0.0733	0.4620	0.0642
Ifthen	0.0469	0.1094	0.0625	0.0938	0.0469	0.1406	0.5000
	$m_1$	$m_2$	$m_3$	$m_4$	$m_5$	$m_6$	$m_7$

Figure 6: Probability distribution of the three logical patterns within the memory structure  $M$ .

We analyze a sample of **275 intermediate conclusions provided by METGEN**, along with their automatically annotated inference types. The distribution of these samples is as follows: **Substitution (153)**, **Conjunction (71)**, and **IF-then (51)**.



1. We introduce a **logical pattern memory pre-trained model** (LMPM), which facilitates the generation of logically consistent intermediate conclusions during entailment steps.
2. LMPM employs an external memory to **learn and retain latent logical patterns** between premises and conclusions. This mechanism significantly enhances the language model's capacity to **capture and utilize logical patterns effectively**.
3. We propose to pre-train the LMPM model via a **constructed entity-abstract dataset**. This approach **mitigates the influence of irrelevant domain knowledge** in the original Wikipedia data and enables the model to be well-trained with less data.
4. we plan to **extend this method to other tasks**, such as the Multimodal QA, and to explore the incorporation of external knowledge to enhance generation

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# Thanks and QA

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Code : <https://github.com/YuanLi95/T5-LMPM>